

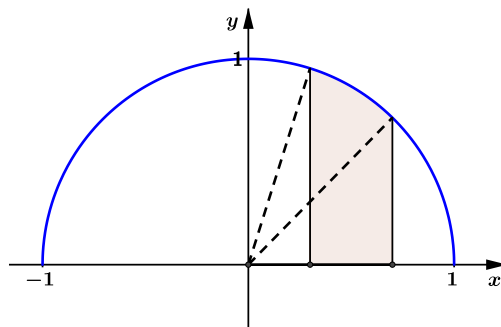
# Circular slice

## Problem

Use the substitution  $x = \cos \theta$  to find

$$\int_a^b \sqrt{1-x^2} dx$$

How does your answer to  $\int_a^b \sqrt{1-x^2} dx$  relate to the following diagram?



# Circular slice

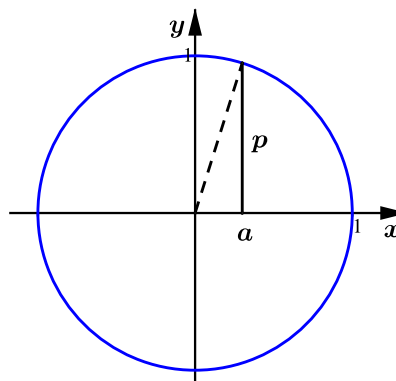
## Suggestion



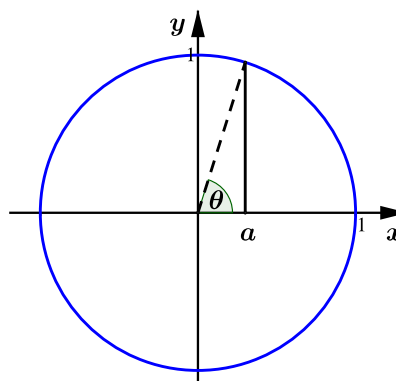
Look carefully at the original diagram. Do you know any information that you can add to the diagram? Are there lengths and areas that you can work out?

Further suggestions can be found by working through the questions below:

(a) Find  $p$  in terms of  $a$ .



(b) Find  $\theta$  in terms of  $a$ .



(c) Find  $\phi$  and the shaded area in terms of  $a$  and  $b$ .



It will be helpful to find the area of the sector using radians rather than degrees.

